Code: IT3T3

II B.Tech - I Semester–Regular/Supplementary Examinations November 2017

PROBABILITY AND STATISTICS (INFORMATION TECHNOLOGY)

Duration: 3 hours

Max. Marks: 70

PART - A

Answer *all* the questions. All questions carry equal marks 11x 2 = 22 M

1.

- a) What are the axioms of probability?
- b) If a random variable has the probability density f(x) as

$$f(x) = \begin{cases} 2e^{-2x}, for \ x > 0\\ 0, for \ x \le 0 \end{cases} \quad \text{then find } p(x \ge 0.5).$$

- c) State Baye's theorem.
- d) A die is tossed thrice. A success is getting 1 or 6 on a toss. Find the mean and variance of the number of successes.
- e) If a random variable has a Poisson distribution such that p(1) = p(2), find the mean of the distribution.
- f) Define population and sample with examples.
- g) A random sample of size 100 has a standard deviation of5. What can you say about the maximum error with 95% confidence.
- h) Define Null & Alternative Hypothesis.
- i) Write the student's t-test for difference of means.

j) For an F-distribution find

i) $F_{0.95}(19,24)$ ii) $F_{0.99}(28,12)$

k) Construct a one way classification of analysis of variance table.

PART – B

Answer any *THREE* questions. All questions carry equal marks. $3 \ge 16 = 48 \text{ M}$

- 2. a) Box I contains 1 white, 2 red, 3 green balls, Box II contains 2 white, 3 red, 1 green balls, Box III contains 3 white, 1 red, 2 green balls. Two balls are drawn from a box chosen at random. These are found to be one white and one red. Determine the probability that the balls so drawn come from box II.
 8 M
 - b) Let X denote the minimum of the two numbers that appear when a pair of fair dice is thrown once. Determine the
 i) Discrete probability distribution
 ii) Expectation
 iii) variance.
- 3. a) Fit a Poisson distribution for the following data and calculate the expected frequencies.8 M

X	0	1	2	3	4
f(x)	109	65	22	3	1

- b) If the masses of 300 students are normally distributed with mean 68kgs and standard deviation 3 kgs, how many students have masses
 i) Greater than 72 kg
 ii) Less than or equal to 64 kg
 iii) Between 65 and 71 kg inclusive.
- 4. a) A normal population has a mean of 0.1 and standard deviation of 2.1. Find the sample size, if maximum error is 1.1372 with 95% confidence.8 M
 - b) The mean and standard deviation of a population are 11,795 and 14,054 respectively. What one can assert that 95% confidence about the maximum error if $\overline{X} = 11,795$ and n=50. And also construct 95% confidence interval for the true mean. 8 M
- 5. a) A die was thrown 9000 times and of these 3220 yielded a 3 or 4. In this consistent with the hypothesis that the die was unbiased.8 M
 - b) Two horses A and B were tested according to the time (in seconds) to run a particular track with the following results

Horse A	28	30	32	33	33	29	34
Horse B	29	30	30	24	27	29	-

8 M

- 6. a) A sample analysis of examination results of 500 students was made. It was found that 200 students had failed, 170 had secured a third class, 90 were placed in second class and 20 got a first class. Do these figures commensurate with the general examination result which is in the ratio of 4:3:2:1 for the various categories respectively.
 - b) The following figures relate to production in kg of three varieties A,B,C of wheat shown in 12 plots.

A	14	16	18	-	-
В	14	13	15	22	-
С	18	16	16	19	20

Test whether the production of wheat of three varieties are equal. 8 M